YEAR 7 — ALGEBRAIC THINKING.

@whisto_maths

Sequences

What do I need to be able to do?

By the end of this unit you should be able

- Describe and continue both linear and non-linear sequences
- Explain term to term rules for linear sequence
- Find missing terms in a linear sequence

ji <u>Keywords</u>

II Sequence: items or numbers put in a pre-decided order

11 Term: a single number or variable

Position: the place something is located

Rule: instructions that relate two variables

Linear: the difference between terms increases or decreases by the same value each time

Non-linear: the difference between terms increases or decreases in different amounts

Difference: the gap between two terms

Orithmetic: a sequence where the difference between the terms is constant

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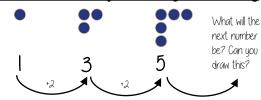
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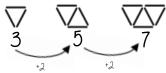
11 Geometric: a sequence where each term is found by multiplying the previous one by a fixed non zero number

Describe and continue a sequence diagrammatically

Count the number of circles or lines in each image



!! Predict and check terms





Predictions:

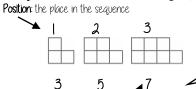
Look at your pattern and consider how it will increase.

eg. How many lines in pattern 67

Prediction - 13

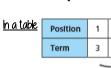
If it is increasing by 2 each time - in 3 more patterns there will be 6 more lines

Sequence in a table and graphically



5 Graphicallu

Term: the number or variable (the number of squares in each image)



Because the terms increase by the same addition each time this is **linear** — as seen in the *grap*h

"The **term** in **position** 3 has 7 squares"

Position

and Fibonacci

• Do not plot as straight lines when modelled graphically

Linear and Non Linear Sequences

The differences between terms can be found by addition, subtraction, multiplication or

13

Linear Sequences — increase by addition or subtraction and the same amount each time

Non-linear Sequences — do not increase by a constant amount — quadratic, geometric

division.

Fibonacci Sequence — look out for this type of sequence

Each term is the sum of the previous two terms.

<u>Continue Linear Sequences</u>

7, 11, 15, 19...

How do I know this is a linear sequence?

It increases by adding 4 to each term.

How many terms do I need to make this conclusion?

Ot least 4 terms — two terms only shows one difference not if this difference is constant (a common difference).

How do I continue the sequence?

You continue to repeat the same difference through the next positions in the seavence

Continue non-linear Sequences

1, 2, 4, 8, 16 ...

How do I know this is a non-linear sequence?

It increases by multiplying the previous term by 2- this is a geometric sequence because the constant is multiply by $2\,$

How many terms do I need to make this conclusion?

Ot least 4 terms — two terms only shows one difference not if this difference is constant (a common difference).

How do I continue the sequence?

You continue to repeat the same difference through the next positions in the sequence.

Explain term-to-term rule How you get from term to term

Try to explain this in full sentences not just with mathematical notation.

Use key maths language — doubles, halves, multiply by two, add four to the previous term etc.

To explain a whole sequence you need to include a term to begin at...





YEAR 7 — ALGEBRAIC THINKING... **Olgebraic notation**

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What do I need to be able to

By the end of this unit you should be able to:

- Be able to use inverse operations and "operation families".
- Be able to substitute into single and two step function machines.
- Find functions from expressions.
- Form sequences from expressions
- Represent functions graphically.

Keywords

Function: a relationship that instructs how to get from an input to an output.

Input: the number/ sumbol put into a function.

Output: the number/ expression that comes out of a function.

Operation: a mathematical process

Inverse: the operation that undoes what was done by the previous operation. (The opposite operation)

Commutative: the order of the operations do not matter.

Substitute: replace one variable with a number or new variable.

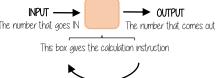
Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

Evaluate: work out

Linear: the difference between terms increases or decreases by the same value each time

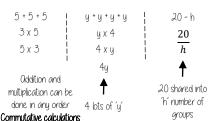
Sequence: items or numbers put in a pre-decided order

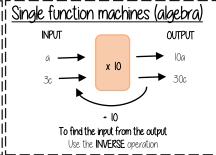
Sinale function machines





Using letters to represent numbers





Find functions from expressions



Find the relationship between the input and the output

Sometimes there can be a number of possible functions e.g. +7x or x 2 could both be solutions to the above function machine

Substitution into expressions



If y = 7 this means the expression is asking for 4 'lots of' 7

4 x 7 OR 7 + 7 + 7 + 7 OR 7 x 4

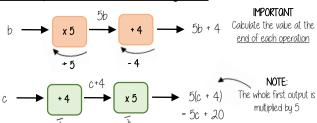
e.a: u-27 - 2 = 5

Two step function machines



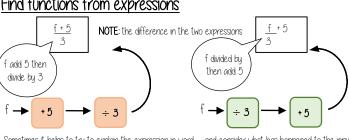
For the input use the **INVERSE** operations

Two step function machines (algebra)

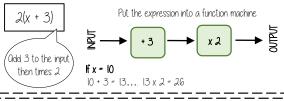


Find functions from expressions

= 28



Substitution into an expression

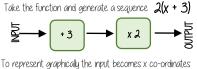


tormina a sequence

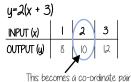
INPUT				
OUTPUT	8	10	12	The substitution is the 'input' val. The OUTPUT becomes the sequer

2(x + 3)

Representing functions graphically

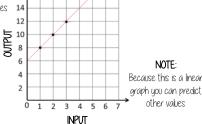


and the output becomes u co-ordinates



(2, 10) to plot on a graph

Not all graphs will be linear only those with an integer value for x. Powers and fractions generate differently shaped graphs



YEAR 7 — ALGEBRAIC THINKING

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Equality and Equivalence

What do I need to be able to do?

By the end of this unit you should be able

- .Form and solve linear equations
- Understand like and unlike terms
- Simplify algebraic expressions

ii Keywords

Equality: two expressions that have the same value

Equation: a mathematical statement that two things are equal

Equals: represented by '=' symbol — means the same

Solution: the set or value that satisfies the equation

Solve: to find the solution.

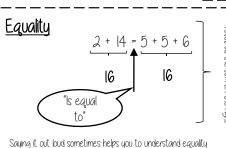
Inverse: the operation that undoes what was done by the previous operation (The opposite operation)

Term: a single number or variable

Like: variables that are the same are 'like'

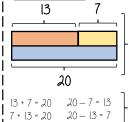
Coefficient: a multiplicative factor in front of a variable e.g. 5x (5 is the coefficient, x is the variable)

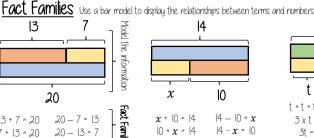
Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

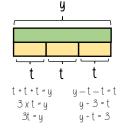


he sum on the left has the san

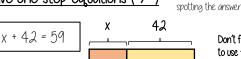
There is more to this than just







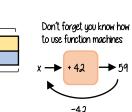
Solve one step equations (+/-)



59

x + 42 = 5942 + x = 59

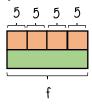
59 - x = 42 59 - 42 = x



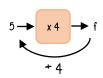
Solve one step equations (x/+)

f = 5f = 4 = 5

f = 5 = 45 x 4 = f



Don't forget you know how to use function machines



_ike and unlike terms

Like terms are those whose variables are he same

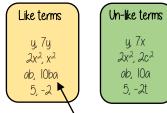




are **unlike** terms

the variables are NOT the same

Examples and non-examples



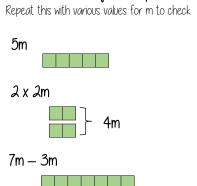
Note here ab and ba are commutative operations, so are still like terms

Equivalence

Check equivalence by substitution e.a. m=10

5m	2 x 2m	7m - 3m
5 x 10	2 x (2x 10)	(7x 10) - (3x 10)
= 50	= 2 x 20	= 70 — 30
	= 40	= 40

Equivalent expressions



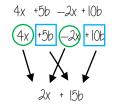
4m

Collecting like terms \equiv symbol

The \equiv symbol means equivalent to. It is used to identify equivalent expressions

Collecting like terms

Only like terms can be combined



Common misconceptions

 $2x + 3x^2 + 4x \equiv$ $6x + .3x^{2}$

Olthough they both have the x variable x2 and x terms are unlike terms so can not be collected

YEAR 7 — PLACE VALUE AND PROPORTION

@whisto maths

Ordering integers and decimals

What do I need to be able to do?

Bu the end of this unit you should be able to:

- Understand place value and the number sustem including decimals Understand and use place value for decimals,
- integers and measures of any size Order number and use a number line for
- positive and negative integers, fractions and
- use the symbols $=, \neq, \leq, \geq$
- Work with terminating decimals and their corresponding fractions
- Round numbers to an appropriate accuracy
- Describe, interpret and compare data distributions using the median and range

Keywords

Opproximate: To estimate a number, amount or total often using rounding of numbers to make them easier to calculate with

Integer: a whole number that is positive or negative Interval: between two points or values

Median: O measure of central tendency (middle, average) found by putting all the data values in order and finding the middle value of the list.

Negative: Only number less than zero; written with a minus sign.

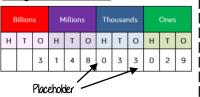
Place holder: We use 0 as a place holder to show that there are none of a particular place in a number

Place value: The value of a digit depending on its place in a number. In our decimal number system, each place is 10 times bigger than the place to its right

Range: The difference between the largest and smallest numbers in a set

Significant figure: O digit that gives meaning to a number. The most significant digit (figure) in an integer is the number on the left. The most significant digit in a decimal fraction is the first non-zero number after the decimal point

Integer Place Value



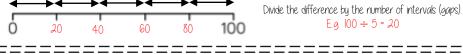
Three billion, one hundred and forty eight million, thirty three thousand and twenty nine

I billion 1, 000, 000, 000

I million 1 000, 000

Decimals

Intervals on a number line



Rounding to the nearest power of ten If the number is halfway between we "round up"

5495 to the nearest 1000 5475 to the nearest 100

5400 (5000) 6000

5475 to the nearest 10 5480

Eq $100 \div 5 = 20$

<u>Compare integers using <,>,=,≠</u>



Spread of the values

Difference between the biggest and smallest

hundredths

Range: Biggest value — Smallest value

Range = 9

П

tenths

Median The middle value

Example 1 Median: put the in order 3 8 find the middle number 3 4 (8) 9 12

Example 2 Median: put the in order

150 154 148

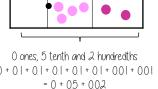
137 160 158 There are 2 middle numbers Find the midpoint

137 148 (150 154)58 160

Round to the first non

zero number

We sau "nought point five two" Five tenths and two



Decimal intervals on a number line

One whole spit into 10 parts makes tenths = 0.1 One tenth split into 10 parts makes hundredths = 0.01

0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9

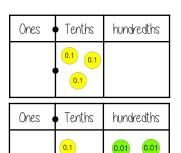
0.02 0.06 0.08 0.04

0 0.2 0.4 0.6 0.8 1 1.2 1.4 1.6 1.8

Comparing decimals

hundreaths

Which the largest of 0.3 and 0.23?



0.3 > 0.23

"There are more counters in the furthest column to the left"

0.30 0.23

Comparing the values both with the same number of decimal places is another way to compare the number of tenths and hundredths

Round to I significant figure

370 to I significant figure is 400

37 to I significant figure is 40 3.7 to I significant figure is 4

0.37 to I significant figure is 0.4

0.0000037 to 1 significant figure is 0.0000004

YEAR 7 - PLACE VALUE AND PROPORTION

@whisto_maths

FDP equivalence

What do I need to be able to do?

By the end of this unit you should be able

Convert fluently between fractions, decimals & percentages

ii Keuwords

Fraction: how many parts of a whole we have

Decimal: a number with a decimal point used to separate ones, tenths, hundredths etc.

Percentage: a proportion of a whole represented as a number between 0 and 100

Place value: the numerical value that a digit has decided by its position in the number

Placeholder: a number that occupies a position to give value Interval: a range between two numbers

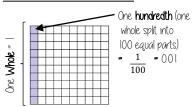
Tenth: one whole split into 10 equal parts

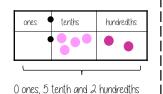
Hundredth: one whole split into 100 equal parts

Sector: a part of a circle between two radius (often referred to as looking like a piece of pie)

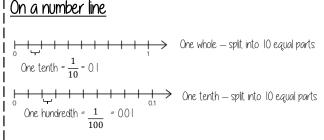
Recurrina: a decimal that repeats in a given pattern

Tenths and hundredths

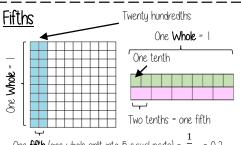


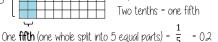


0 + 0 | + 0 | + 0 | + 0 | + 0 | + 0 | + 0 | | = 0 + 0.5 + 0.02 = 0.52

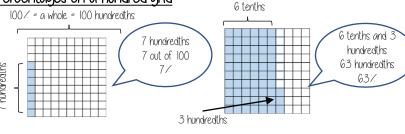


One tenth (one whole split into 10 equal parts) =





Percentages on a hundred grid

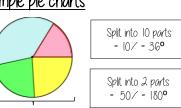


Quarters One **quarter** (one whole split into 4 equal parts) = $\frac{1}{4}$ Twenty five hundreaths Whole One half



a pie chart has 360°

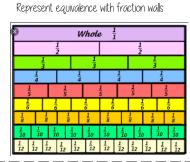
so all FDP calculations





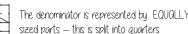
Split into 5 parts

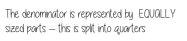
= 20% = 72°

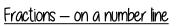


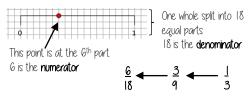
Equivalent fractions

Fractions — on a diagram



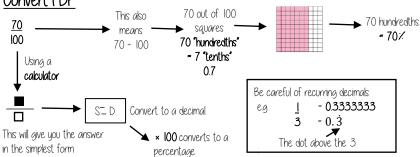








are out of 360



FAR 7 — APPLICATION OF NUMBER

Solving problems with addition and subtraction

What do I need to be able to do?

I By the end of this unit you should be able to:

- Understand properties of addition/subtraction
- Use mental strategies for addition/subtraction
- Use formal methods of addition/Subtraction for integers
- Use formal methods of addition/Subtraction for decimals |
- Solve problems in context of perimeter
- Solve problems with finance, tables and timetables
- Solve problems with frequency trees
- Solve problems with bar charts and line charts

Keywords

Commutative: changing the order of the operations does not change the result

Ossociative: when you add or multiply you can do so regardless of how the numbers are grouped

Inverse: the operation that undoes what was done by the previous operation. (The opposite operation) Placeholder: a number that occupies a position to give value

Perimeter: the distance/length around a 2D object

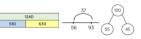
Polyaon: a 2D shape made with straight lines

i Balance: in financial questions — the amount of money in a bank account

I | Credit: money that goes into a bank account

I Debit: money that leaves a bank account

Oddition/Subtraction with integers



Modelling methods for addition/subtraction

- Bar models
- Number lines
- Part/Whole diagrams





The order of addition does not change the result

Subtraction the order has to stay the same



- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/subtraction
- Show your relationships by writing fact families

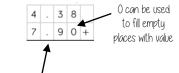
8 cm

Formal written methods

MILLERI MELHOUS							
	Т	0			Н	Т	О
	8	7			4	2	7
	4	2		_	2	4	9

Remember the place value of each column. You may need to move 10 ones to the ones column to be able to subtract

Oddition/Subtraction with decimals



The decimal place acts as the placeholder and aligns the other values



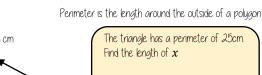
Revisit Fraction — Decimal equivalence

Solve problems with perimeter

Isosceles

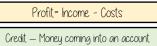
Triangle

notation



8cm + 8cm + xcm = 25cm16cm + xcm = 25cmxcm = qcm

Solve problems with finance



Debit — Money leaving an account

Money uses a two decimal place system. 14.2 on a calculator represents £14.20

Check the units of currency — work in the same

Tables and timetables

Distance tables London

	211	Cardiff		
ŀ	(556)	493	Glasgow	
4	518	392	177	
_				

This shows the distance between Glasgow and London. It is where their row and column intersects Bus/ Train timetables

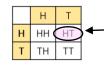
x cm

			. 1
1005	1045	1130	
1024	1106	1147	
1051	1133	1205	
1117	1202	1233	4
	1024	1024 1106 1051 1133	1024 1106 1147 1051 1133 1205

Each column represents a journey, each row represents the time the 'bus' arrives at that location

TIME COLCUOLTIONS — use a number line

Two-way tables



Where rows and columns intersect is the outcome of that action

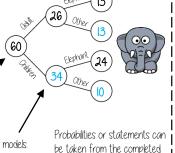
Frequency trees

60 people visited the zoo one Saturdau morning.

26 of them were adults. 13 of the adult's favourite animal was an elephant. 24 of the children's favourite animal was an

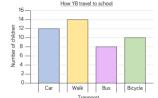
The overall total "60 people"

a frequency tree is made up from part-whole models. One piece of information leads to another



e.g. 34 children visited the zoo

Bar and line charts



Use addition/subtraction methods to extract information from bar charts.

eg Difference between the number of students who waked and took the bus. Walk frequency — bus frequency

When describing changes or making predictions.

- Extract information from your data source
- Make comparisons of difference or sum of values.
- Put into the context of the scenario

R 7 — APPLICATION OF NUMBER

Solving problems with multiplication and division

What do I need to be able to do?

By the end of this unit you should be able to:

- Understand and use factors
- Understand and use multiples
- Multiply/ Divide integers and decimals by powers
- Use formal methods to multiply
- Use formal methods to divide
- Understand and use order of operations
- Solve area problems
- Solve problems using the mean

Keywords

Orrau: an arrangement of items to represent concepts in rows or columns

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number.

Mili: prefix meaning one thousandth

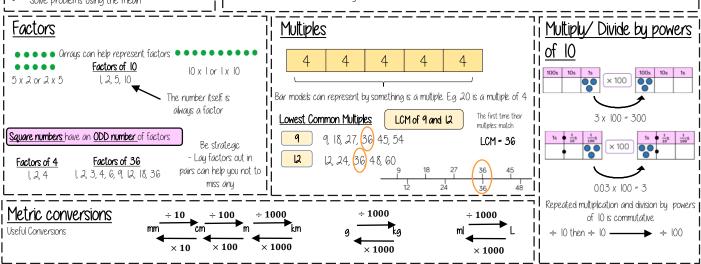
Centi: prefix meaning one hundredth.

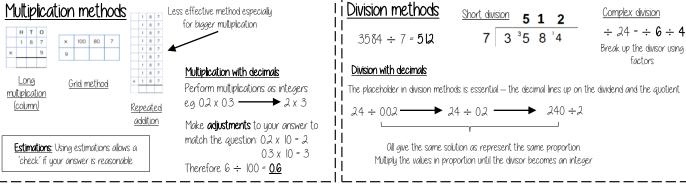
Kilo: prefix meaning multiply by 1000

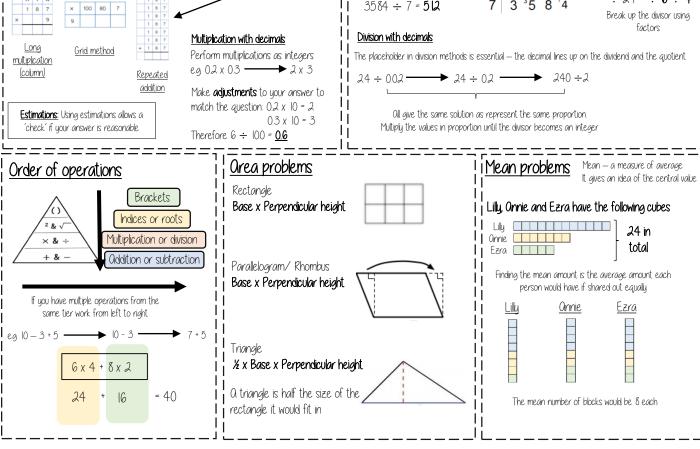
Quotient: the result of a division

Dividend: the number being divided

Divisor: the number we divide by.







YFAR 7 - APPLICATION OF NUMBER

Fractions and percentages of amounts

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Find a fraction of a given amount
- Use a given fraction to find the whole or other fractions
- Find the percentage of an amount using mental methods
- Find the percentage of a given amount using a calculator

Keywords

Fraction: how many parts of a whole we have

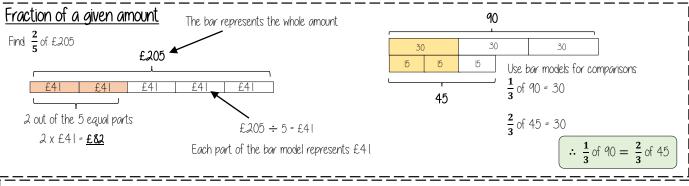
Equivalent: of equal value

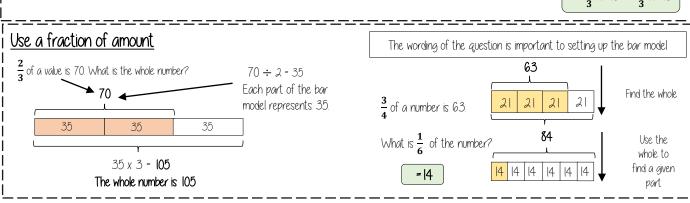
Whole: a number with no fractional or decimal part.

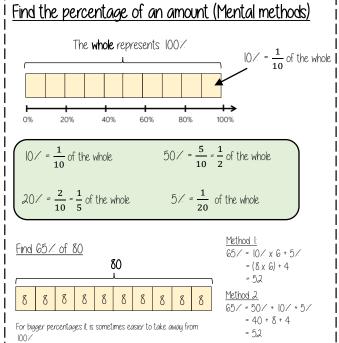
Percentage: parts per 100 (uses the / symbol)

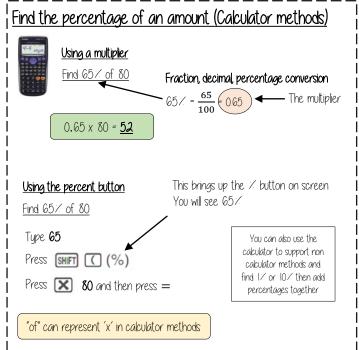
Place Value: the value of a digit depending on its place in a number. In our decimal number system, each place is 10 times bigger than the place to its right

Convert: change into an equivalent representation, often fraction to decimal to a percentage cycle.









YEAR 7 — DIRECTED NUMBER

Operations with equations and directed numbers

What do I need to be able to do?

By the end of this unit you should be able to:

- Perform calculations that cross zero
- Odd/ Subtract directed numbers
- Multiplu/ Divide directed numbers
- Evaluate algebraic expressions
- Solve two-step equations
- Use order of operations with directed number

| <u>Keywords</u>

Subtract: taking away one number from another.

Negative: a value less than zero.

Commutative: changing the order of the operations does not change the result

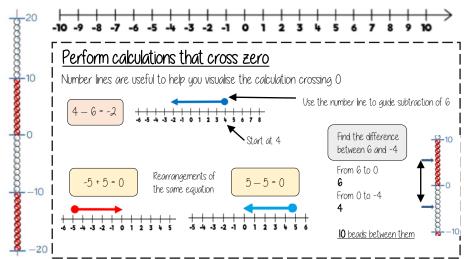
Product: multiply terms

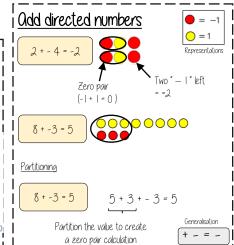
Inverse: the opposite function

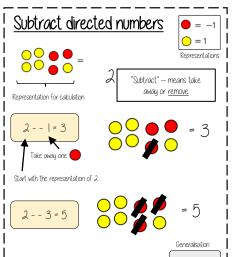
| **Square root**: a square root of a number is a number when multiplied by itself gives the value (symbol $\mathcal F$)

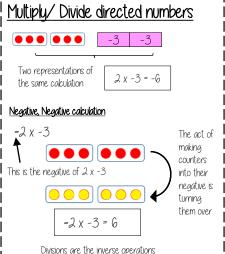
Square: a term multiplied by itself.

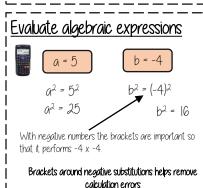
Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

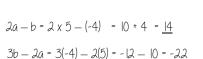


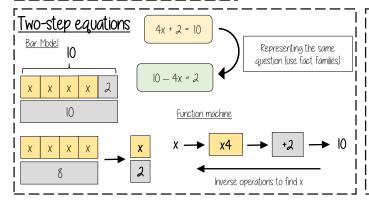


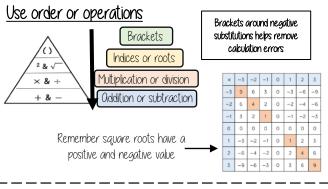












FAR 7 — FRACTIONAL THINKING

Addition and subtraction of fractions

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What do I need to be able to do?

By the end of this unit you should be able to:

- Convert between mixed numbers and fractions
- Odd/Subtract unit fractions (same denominator)
- Odd/Subtract fractions (same denominator)
- Odd/Subtract fractions from integers
- Use equivalent fractions Odd/Subtract any fractions
- Odd/Subtract improper fractions and mixed
- Use fractions in algebraic contexts

Keywords

Numerator: the number above the line on a fraction. The top number. Represents how many parts are taken.

Denominator: the number below the line on a fraction. The number represent the total number of parts

Equivalent: of equal value

Mixed numbers: a number with an integer and a proper fraction

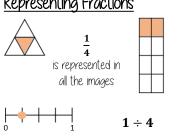
Improper fractions: a fraction with a bigger numerator than denominator

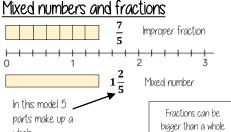
Substitute: replace a variable with a numerical value

Place value: the value of a digit depending on its place in a number. In our decimal number system, each place is

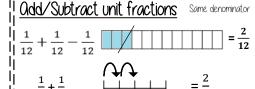
10 times bigger than the place to its right

Representing Fractions



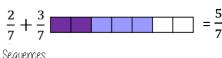




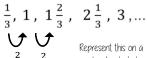


With the same denominator ONLY the numerator is added

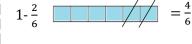
Odd/Subtract fractions



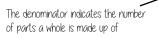


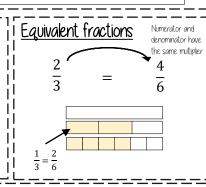


Same denominator | | Odd/Subtract from integers

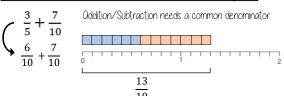




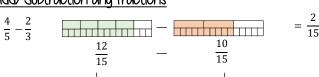




Odd/Subtraction fractions (common multiples)

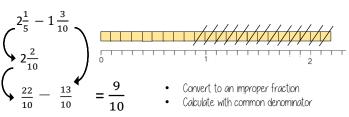


Odd/Subtraction any fractions



Use equivalent fractions to find a common multiple for both denominators

Odd/Subtraction fractions (improper and mixed)



Partitioning method

$$2\frac{1}{5} - 1\frac{3}{10} = 2\frac{2}{10} - 1\frac{3}{10} = 2\frac{2}{10} - 1 - \frac{3}{10} = 1\frac{2}{10} - \frac{3}{10} = \frac{9}{10}$$

Fractions in algebraic contexts

$$k - \frac{5}{8} = 2$$

$$5 \longrightarrow \frac{7}{9}$$

$$\frac{2}{3}$$

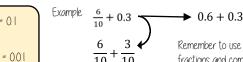
Apply inverse operations

Form expressions with fractions

Substitution

 $p = 5 \ m = 2$

Fractions and decimals



Remember to use equivalent fractions and common denominators

YEAR 7 — LINES AND ANGLES

Constructing, measuring and using geometric notation

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What do I need to be able to do?

By the end of this unit you should be able to:

- Use letter and labelling conventions
- Draw and measure line segments and angles
- Identify parallel and perpendicular lines
- Recognise types of triangle
- Recognise types of quadrilateral
- Identify polygons
- Construct triangles (SQS, SSS, QSQ)
- Draw Pie charts

Keuwords

Polygon: a 2D shape made with straight lines

Scalene triangle: a triangle with all different sides and angles

Isosceles triangle: a triangle with two angles the same size and two angles the same size

Right-angled triangle: a triangle with a right angle Frequency: the number of times a data value occurs

Sector: part of a circle made by two radii touching the centre

Rotation: turn in a given direction

Protractor: equipment used to measure angles

Compass: equipment used to draw arcs and circles.



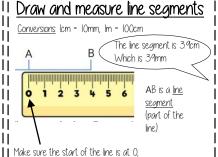
The letter in the middle is the angle The arc represents the angle

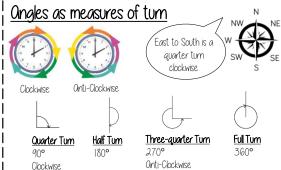


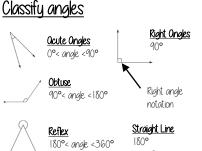
Onale Notation: three letters ABC

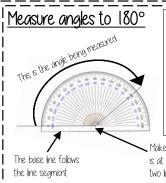
This is the angle at B = 113°

Line Notation: two letters EC The line that joins E to C









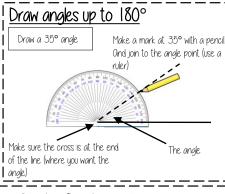
li Draw Pie Charts

Remember to use estimation This is an obtuse anale so between 90° and 180° Make sure the cross is at the point the two lines meet

Read from 0°

on the base

line.



Parallel and Perpendicular lines

Parallel lines

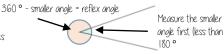
Straight lines that never meet (Have the same gradient)

<u>Perpendicular lines</u>

Straight lines that meet at 90°

Ongles over 180°

Use your knowledge of straight lines 180° and angles around a point



Properties of Quadrilaterals

=========



Oll angles 90° Opposite sides are parallel

Rectangle

Rhombus Oll sides equal size Opposite angles are equal

<u>Parallelogram</u>

Opposite sides are parallel Opposite angles are equal Co-interior angles

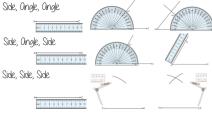
One pair of parallel lines

<u>Kite</u>

No parallel lines Equal lengths on top sides 1 Equal lengths on bottom sides One pair of equal angles

"32 out of 60 people had a dog" This fraction of the 360 degrees represents doas Use a protractor to draw This is 192° <u>32</u> x 360 = 192°

SQS, SSS, QSQ constructions Side, Ongle, Ongle



Polygons

Triangle

- Quadrilateral

- Pentagon - Hexagon
- Octagon - Nonagon - Heptagon - Decagon
- If all the sides and angles are the same, it is a reaular polygon

YEAR 7 — LINES AND ANGLES

@whisto maths

Geometric reasoning

What do I need to be able to do?

By the end of this unit you should be able to:

- Understand/use the sum of angles at a point
- Understand/use the sum of angles on a straight line.
- Understand/use equality of vertically opposite anales
- Know and apply the sum of angles in a triangle
- Know and apply the sum of angles in a quadrilateral

Keywords

Vertically Opposite: angles formed when two or more straight lines cross at a point.

Interior Ongles: angles inside the shape

Sum: total, add all the interior angles together

Convex Quadrilateral: a four-sided polygon where every interior angle is less than 180°

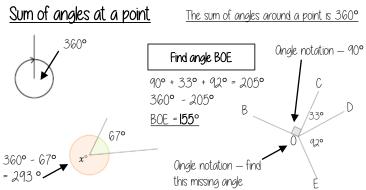
Concave Quadrilateral: a four-sided polygon where one interior angle exceeds 180°

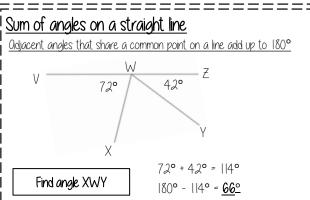
Polygon: 0 2D shape made with straight lines

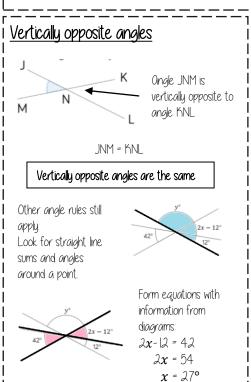
Scalene triangle: a triangle with all different sides and angles

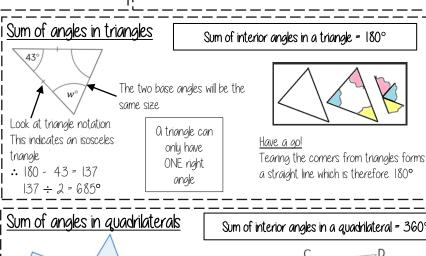
I isosceles triangle: a triangle with two angles the same size and two angles the same size

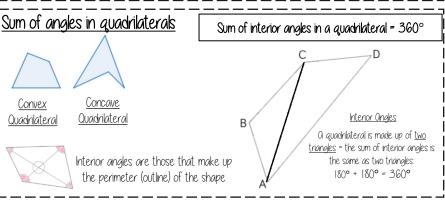
I | Right-angled triangle: a triangle with a right angle

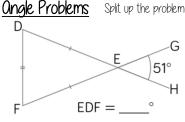












Split up the problem into chunks and explain your reasoning at each point using angle notation

l Ongle DEF = $5\,\mathrm{l}^\circ$ because it is a vertically opposite angle DEF = GEH

2. Triangle DEF is isosceles (triangle notation) : EDF = EFD and the sum of interior angles is 180° $180^{\circ} - 51^{\circ} = 129^{\circ}$ $129^{\circ} \div 2 = 645^{\circ}$

3. Ongle EDF = 64.5°

Keep working out clear and notes together

YFAR 7 - REASONING WITH NUMBER

@whisto maths

Developing number sense

What do I need to be able to do?

By the end of this unit you should be able to:

- Know and use mental addition/subtraction
- Know and use mental multiplication/division
- Know and use mental arithmetic for decimals
- Know and use mental arithmetic for fractions
- Use factors to simplify calculations
- Use estimation to check mental calculations
- Use number facts
- Use algebraic facts

Keywords

Commutative: changing the order of the operations does not change the result

Ossociative: when you add or multiply you can do so regardless of how the numbers are grouped

Dividend: the number being divided

Divisor: the number we divide by.

Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign

Equation: a mathematical statement that two things are equal

Quotient: the result of a division

Mental methods for addition/subtraction

Oddition is commutative

Subtraction the order has to stay the same II Multiplication is commutative



The order of addition does not change the result

- 360 147 = 360 100 40 7
- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/subtraction

¦¦Mental methods for multiplication∕ division



 $2 \times 4 = 4 \times 2$

The order of multiplication does not change the result

Partitioning can help multiplication

$$24 \times 6 = 20 \times 6 + 4 \times 6$$

= $120 + 24$

= |44

Division is not associative

Chunking the division can help $4000 \div 25$ "How many 25's in 100" then how many chunks of that in 4000.

Mental methods for decimals

Multiplying by a decimal < I will make the original value smaller e.g x 0.1 = + 10

Methods for multiplication 12×0.03

 $12 \times 3 = 36$ $1.2 \times 3 = 3.6$ $1.2 \times 0.3 = 0.36$ $1.2 \times 0.03 = 0.036$

 $12 \times 3 = 36$ ÷ 10 ÷ 100 ÷ 1000 $1.2 \times 0.03 = 0.036$

Methods for addition 23+24

0.3 + 0.4 = 0.74 + 0.7 = 4.7

Methods for division $15 \div 0.05$

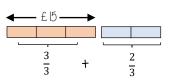
Multiply by powers of 10 until the divisor becomes an integer

1.5 ÷ 0.05 ×100

Mental methods for fractions

Use bar models where possible





What is $\frac{5}{3}$ of £ 15?

£ 14

Using factors to simplify calculations

30 x 16

10 x 3 x 4 x 4

2x5x3x2x2x2x2

10 x 3 x 2 x 8

16 x 10 x 3

Multiplication is commutative Factors can be multiplied in any order

Estimation

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

Most estimations round to I significant figure

Estimations are useful — especially when using fractions and decimals to check if your solution is possible.

210 + 899 < 1200

This is true because even if both numbers were rounded up, they would reach 300 + 900

> The correct estimation would be 200 + 900 = 1100.

Number facts

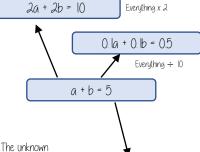
124 x 5 = 620

For multiplication, each value that is multiplied or divided by powers of 10 needs to happen to the result

620÷ 124 = 50

For division you must consider the impact of the divisor becoming smaller or bigger. Smaller — the answer will be bigger (It is being shared into less parts) Bigger — the answer will be smaller (It is being shared into more parts)

¦i Olgebraic facts



quantity isn't changing but the variables change what is done to give the result

Odd 2 to the total a + b + 2 = 7

YFAR 7 — REASONING WITH NUMBER

@whisto maths

Sets and probability

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify and represent sets
- Interpret and create Venn diagrams
- Understand and use the intersection of sets
- Understand and use the union of sets
- Generate sample spaces for single events
- Calculate the probability of a single event
- Understand and use the probability scale

Keywords

Set: collection of things

Element: each item in a set is called an element

Intersection: the overlapping part of a Venn diagram (QND \cap)

Union: two ellipses that join (OR U)

Mutually Exclusive: events that do not occur at the same time

Probability: likelihood of an event happening

Bias: a built-in error that makes all values wrong (unequal) by a certain amount, e.g. a weighted dice

Fair: there is zero bias, and all outcomes have an equal likelihood

Random: something happens by chance and is unable to be predicted.

ldentify and represent sets

The **universal set** has this symbol ξ — this means EVERYTHING in the Venn diagram is in this set

a set is a collection of things — you write sets inside curly brackets { }

 ξ = {the numbers between | and 50 inclusive}

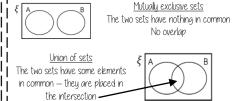
My sets can include every number between and 50 including those numbers

A = {Square numbers}

A = {1, 4, 9, 16, 25, 36, 49}

Oll the numbers in set A are square number and between Land 50

Interpret and create Venn diagrams





Oll of set B is also in Set O so the ellipse fits inside the set.



Oround the outside of every Venn diagram will be a box. If an element is not part of any set it is placed outside an ellipse but inside, the box

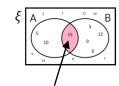
Intersection of sets

Elements in the intersection are in set $m{A}$ QND set B

The notation for this is $A \cap B$

 ξ = {the numbers between | and | 15 inclusive}

 $A = \{\text{Multiples of 5}\}$ $B = \{\text{Multiples of 3}\}$



The element in $A \cap B$ is 15

In this example there is only one number that is both a multiple of 3 and a multiple of 5 between 1 and 15

Jnion of sets

Elements in the union could be in set $oldsymbol{A}$ OR set

The notation for this is $A \cup B$



 ξ = {the numbers between 1 and 15 inclusive}

 $A = \{\text{Multiples of 5}\}$ $B = \{\text{Multiples of 3}\}$

The elements in $A \cup B$ are 5, 10, 15, 3, 9, 6, 12

yellow balls, so

they have the

same probability

There are 7 elements that are either a multiple of 5 OR a multiple of 3 between 1 and 15

Sample space — for single events

a sample space for rolling a six-sided dice is S={1,2,3,4,5,6}

S = {Pink. Blue. Yellow}

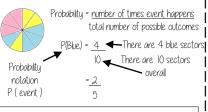
O sample space for this spinner is

- O Sample space represents a possible outcome from an event
- They can be interpreted in a variety of ways because they do not tell you the probability

This Venn shows the number of elements in each set

You only need to write each element once in a sample space diagram

Probability of a single event

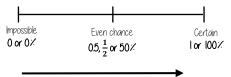


Probability can be a fraction, decimal or percentage

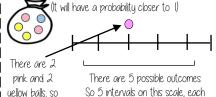
= 40 . = ()4() = 4()/

Probability is always a value between 0 and 1

The probability scale



The more likely an event the further up the probability it will be in comparison to another event



interval value is $\frac{1}{5}$

11 Sum of probabilities

Probability is always a value between 0 and 1



The probability of getting a blue ball is 🕺 :The probability of **NOT** getting a blue ball is $\frac{4}{5}$

The sum of the probabilities is I

The table shows the probability of selecting a type of chocolate

Dark	Milk	White
0.15	0.35	

P(white chocolate) = 1 - 0.15 - 0.35



YEAR 7 — REASONING WITH NUMBER

@whisto maths

Prime numbers and Proof

What do I need to be able to do?

By the end of this unit you should be able to:

- Find and use multiples
- Identify factors of numbers and expressions
- Recognise and identify prime numbers
- Recognise square and triangular numbers
- Find common factors including HCF
- Find common multiples including LCM

Keywords

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number.

Prime: an integer with only 2 factors.

Conjecture: a statement that might be true (based on reasoning) but is not proven.

Counterexample: a special tupe of example that disproves a statement.

Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

Product of prime factors

Multiplication

part-whole

I HCF: highest common factor (biggest factor two or more numbers share)

I LCM: lowest common multiple (the first time the times table of two or more numbers match)

